

AAAI-24 Symposium Spring Symposium on User-Aligned Assessment of Adaptive AI Systems

Can LLMs translate <u>SAT</u>isfactorily? Assessing LLMs in Generating and Interpreting Formal Specifications

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Presenter



Introduction

- Language Models (LMs) have been shown to be successful in a myriad of tasks
 - Natural Language Translation
 - Text Summarization
 - Question Answering
 - Named Entity Recognition

• ...

- Recently, the advent of Large Language Models (LLMs) like ChatGPT have extended the list of applications
 - Code Generation
 - Code Explanation

Introduction

• Language Models (LMs) have h of tasks

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- Natural Language Trans'
- Text Summarization
- Question Answ March 12th, 2024 Whitten by Scott Wu
- Named Er+'
- Cognition • Rec have

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- Coc
- Code

Introducing Devin, the first Al software And setting a new state of the art on the SWE-bench coding benchmark age Models (LLMs) like ChatGPT

Aboutus

BIOB

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Motivation

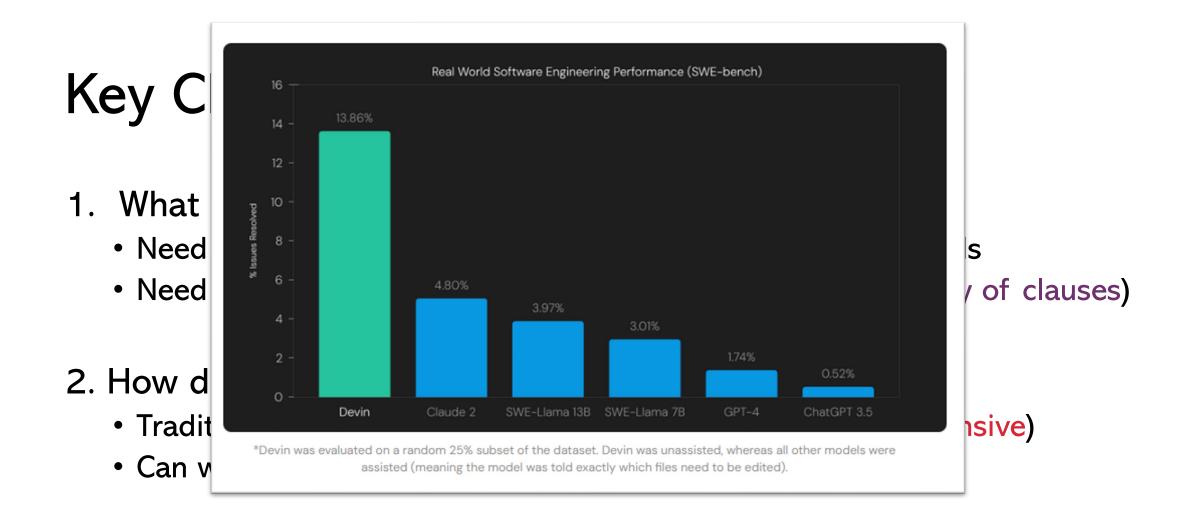
- Increasing interest in using LLMs in system synthesis/explanation
 - Needs LLMs to generate/translate formal syntax (e.g. source code)

Q: Can we use LLMs for generating/interpreting formal syntax?

How do you create a scalable benchmark for testing LLMs?

Key Challenges

- 1. What datasets to use?
 - Need datasets that are not already in the training set of LLMs
 - Need datasets that can be well-characterized (e.g. complexity of clauses)
- 2. How do we automatically evaluate LLMs?
 - Traditionally, humans annotate ground-truth data (very expensive)
 - Can we do this automatically?



(Large) Language Models: (L)LMs

Given an input x consisting of a sequence of tokens, a (large) language model, $p_{\theta}(x)$, parameterized by θ , returns a sequence of tokens $y \sim p_{\theta}(y|x')$.

- The input x is known as a prompt (usually contains the input and question)
- The output y is conditioned on the context window size x'
 - Critical for performance (serves as short-term memory)

You

Summarize the following text using one sentence.

Al systems are increasingly interacting with users who are not experts in Al. This has led to growing calls for better safety assessment and regulation of Al systems. However, broad questions remain on the processes and technical approaches that would be required to conceptualize, express, manage, and enforce such regulations for adaptive Al systems, which by nature, are expected to exhibit different behaviors while adapting to evolving user requirements and deployment environments.

This symposim will foster research and development of new paradigms for assessment and design of AI systems that are not only efficient according to a task-based performance measure, but also safe to use by diverse groups of users and compliant with the relevant regulatory frameworks. It will highlight and engender research on new paradigms and algorithms for assessing AI systems' compliance with a variety of evolving safety and regulatory requirements, along with methods for expressing such requirements.

We also expect that the symposium will lead to a productive exchange of ideas across two highly active fields of research, viz., AI and formal methods. The organization team includes active researchers from both fields and our pool of invited speakers features prominent researchers from both areas.

Please feel free to send workshop related queries at: aia2024.symposium@gmail.com.

ChatGPT

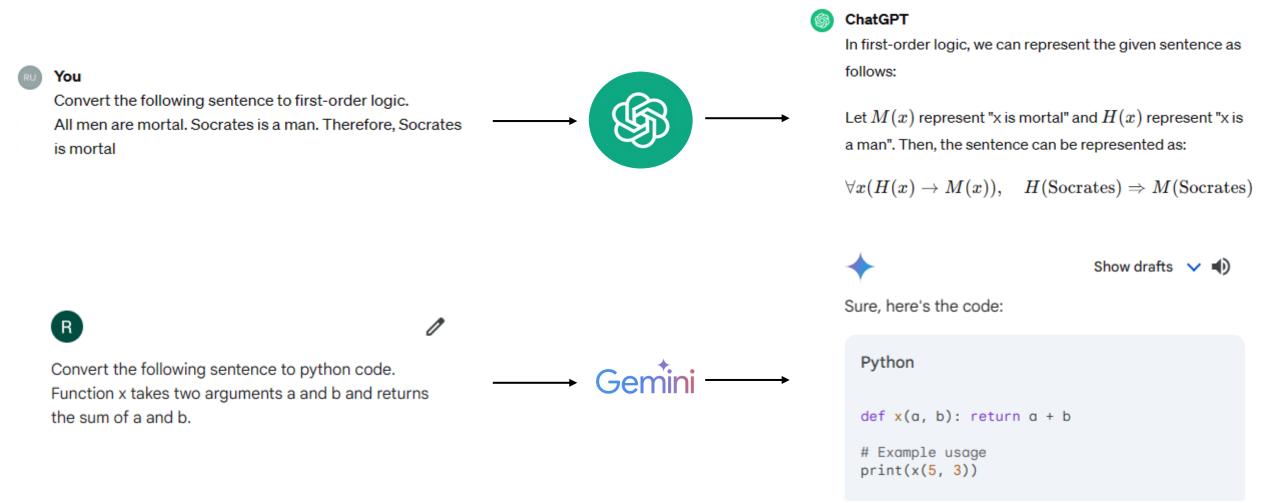
The text discusses the increasing need for better safety assessment and regulation of AI systems due to their growing interaction with non-expert users, while proposing a symposium to promote research on new paradigms for designing AI systems that are efficient, safe, and compliant with regulatory frameworks, aiming to foster collaboration between AI and formal methods researchers.

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Formal Syntax Translation: $NL \rightarrow SAT$

Given an input prompt NL in natural language, $NL \rightarrow SAT$ converts NL to formal syntax SAT s.t. SAT accurately represents NL



Formal Syntax Interpretation: $SAT \rightarrow NL$

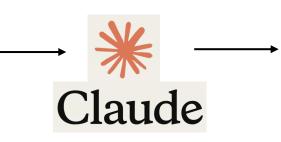
Given an input prompt *SAT* in formal syntax, $SAT \rightarrow NL$ converts *SAT* to natural language *NL* s.t. *NL* accurately represents *SAT*



Explain the following propositional formula:

(p1 and (p2 or (not p3))

Be concise in your response.



The formula represents the conjunction of proposition p1 with a disjunction where either p2 is true or the negation of p3 is true. For the entire formula to be true, p1 must be true, and at least one of p2 or the negation of p3 must be true.

You

Explain the following PDDL action concisely: (:action grasp :parameters (?gripper - gripper ?object - object)

:precondition (and (empty ?gripper))

:effect (and (holding ?object) (not (empty ?gripper))))



ChatGPT

This PDDL action defines the "grasp" action, which takes a gripper and an object as parameters. It can only be executed if the gripper is empty, and upon execution, it makes the gripper hold the object while marking the gripper as not empty.

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Our Contributions

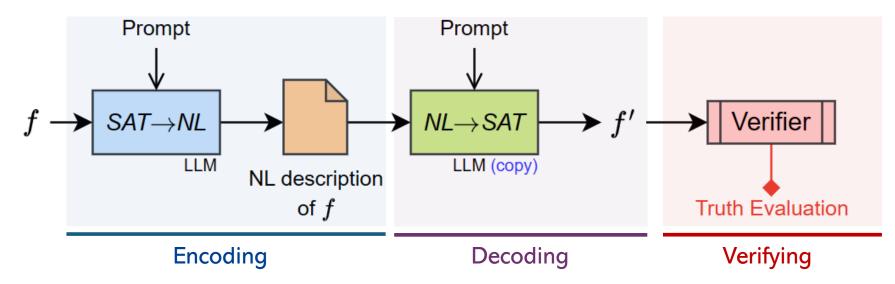
We present an approach for automatic evaluation of $NL \leftrightarrow SAT$

- 1. Automatic, ground-truth data generation
 - We generate data using the grammar of the formal language being tested
 - Formulae variables are perturbed to generate OOD data
- 2. Two LLM copies for automatic evaluation of $NL \leftrightarrow SAT$
 - We use an encoder-decoder scheme for automatic evaluation of $NL \leftrightarrow SAT$
 - No human input required in the process

3. Extensive empirical evaluation

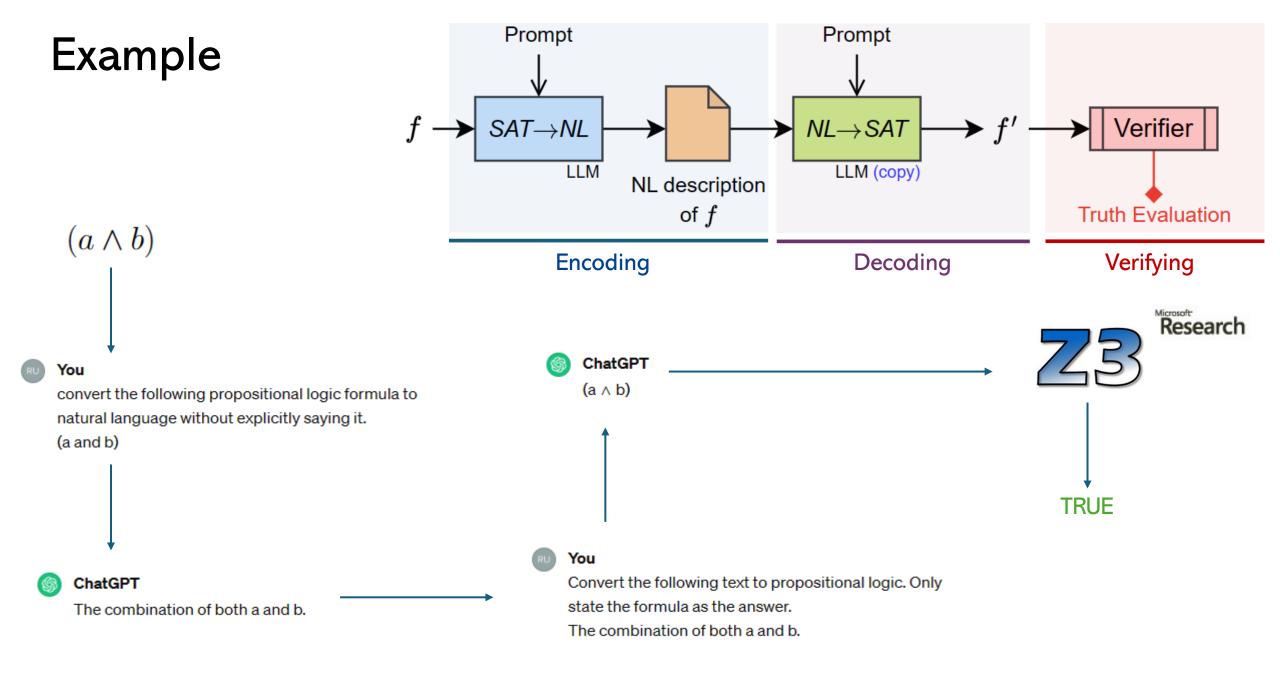
• We present an extensive evaluation using several SOTA LLMs

Automatic Assessment of $NL \leftrightarrow SAT$ using LLMs



Given a statement f in formal syntax, we

- a) Encoding: Convert it to an NL description X using $SAT \rightarrow NL$ using an LLM
- b) Decoding: We use a copy of the LLM to convert X to formal syntax f' using $NL \rightarrow SAT$
- c) Verifying: We use a verifier (such as a theorem prover) to check if $f \equiv f'$

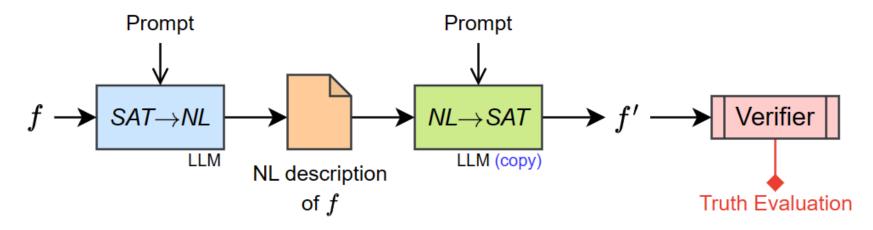


Scalable Datasets

 $\begin{aligned} \mathcal{G}_{fol} &: f \to q, \dots s | s \\ q \to \forall \text{variable} | \exists \text{variable} \\ s \to \text{predicate} | \text{predicate}(t, \dots) | s \lor s | s \land s | \neg s \end{aligned}$ $\begin{aligned} \text{predicate} \to p_1 | p_2 | \dots \\ t \to \text{constant} | \text{variable} \\ \text{constant} \to X_1 | X_2 | \dots \end{aligned}$ $\begin{aligned} \text{variable} \to x_1 | x_2 | \dots \end{aligned}$

- Generated using language grammars
 - Can be scaled up easily (without requiring human annotation) as LLM capabilities evolve
- Can be stratified easily based on type of language produced
 - Example: k-SAT propositional logic formulae

No/Minimal Human Input Needed



- Humans either not required at any point in the pipeline or trivially required
 - Example: Setting up parameters of the dataset generation etc.

Robust against Hallucinations

RU	You	RU	You
	is (a or c) the simplified version of the propositional logic formula: a or ((not b) and c)		is (a or c) the simplified version of the propositional logic formula: a or ((not b) and c)
	answer yes or no		answer yes or no
	0		Ø
\$	ChatGPT	\$	ChatGPT
	No		Yes.

- Many techniques (in contrast to ours), use LLMs as a self-critique verifier
- We use well-defined reasoning processes (external verifier) for truth evaluation
 - This makes our approach less susceptible to hallucinations

Experiments

- We performed an empirical evaluation with two popular forms of formal syntax
 - 1. Propositional logic
 - 2. First-order logic
- We used several SOTA LLMs in our evaluation
 - 1. ChatGPT (GPT-3.5-turbo)
 - 2. GPT-4
 - 3. Gemini (Pro)
 - 4. Mistral (7B Instruct)

Our results show that LLMs are currently not suitable for deployment in formal specification-based tasks.

Propositional Logic

A statement or formula in propositional logic consists of a set of propositions connected together with logical connectives

• We used Z3 to validate whether $f_1 \equiv f_2$ for two formulae: f_1, f_2

Prompt Engineering

- LLM performance quite often depends upon the prompt
- We ensured the efficacy of our prompts by testing different prompts on (k, m)-CNF (Canonical Normal Form) formulae:

(k, m)-CNF formulae are propositional logic formulae expressed as

 $f = f_1 \land \ldots \land f_m$ where $f_i = p_1 \lor \ldots \lor p_k \text{ with } p_i \in \{x_i, \neg x_i\} \text{ where } x_i \text{ is}$ a proposition from the set $\{x_1, \ldots, x_n\}$

• We tested different prompts on a dataset of 400 such formulae with k = 3, n = 3, and $m \in [3, 21]$ until at least one LLM had $\geq 95\%$ accuracy on $NL \leftrightarrow SAT$

• For a given k, m, the formula has (k - 1)m operators.

Dataset Generation

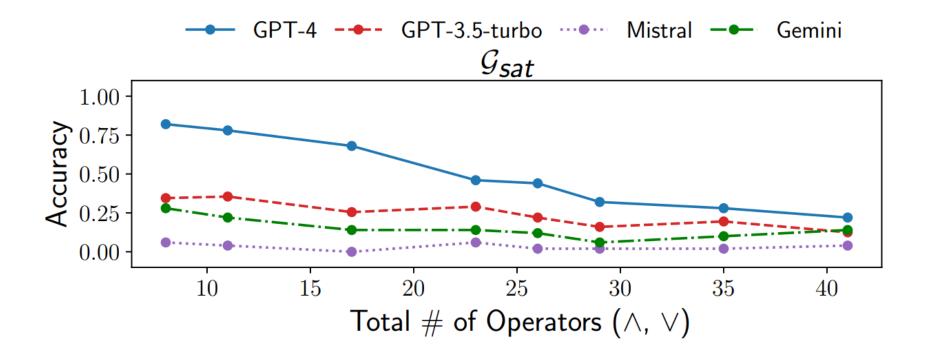
We used the following grammar for generating formulae:

 $\mathcal{G}_{sat}: p \to x | p \lor p | p \land p | \neg p$

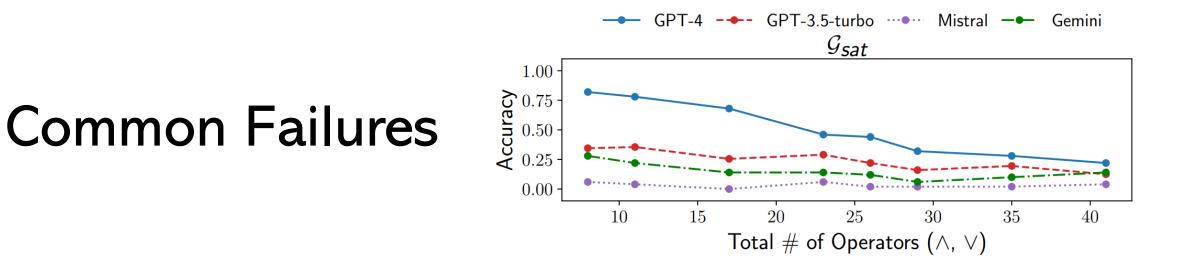
- Similar formula sizes as those in prompt engineering step
 - # of operators used as metric for generating formulae.

• We used Z3 as the verifier for testing logical equivalence

Results: (5 runs, higher values better)



- GPT-4 outperforms other LLMs
- LLMs cannot perform $NL \leftrightarrow SAT$ satisfactorily in propositional logic



$NL \rightarrow SAT$ failures

- One key failure was unable to capture the parentheses correctly
- Another was a bias from the LLMs knowledge based wherein it used symbols other than those in the prompt (e.g. →)

 $SAT \rightarrow NL$ failures

Assuming $SAT \rightarrow NL$ was correct and a human could correctly decode the NL expression

• LLMs like Gemini would often hallucinate during this phase

First-order Logic (FOL)

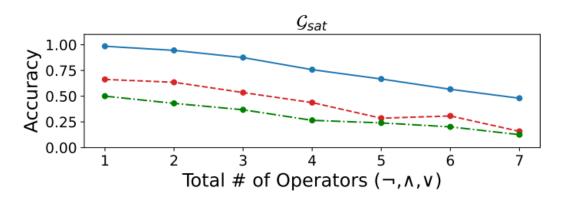
A statement or formula in first-order logic consists of a set of predicates connected together with logical connectives and quantifiers

 $\begin{aligned} \mathcal{G}_{fol} &: f \to q, \dots s | s \\ q \to \forall \text{variable} | \exists \text{variable} \\ s \to \text{predicate} | \text{predicate}(t, \dots) | s \lor s | s \land s | \neg s \end{aligned}$ $\begin{aligned} \text{predicate} \to p_1 | p_2 | \dots \\ t \to \text{constant} | \text{variable} \\ \text{constant} \to X_1 | X_2 | \dots \end{aligned}$ $\begin{aligned} \text{variable} \to x_1 | x_2 | \dots \end{aligned}$

We used a similar prompt engineering step for FOL.

Results: Randomized predicates

--- GPT-4 --- GPT-3.5-turbo --- Gemini

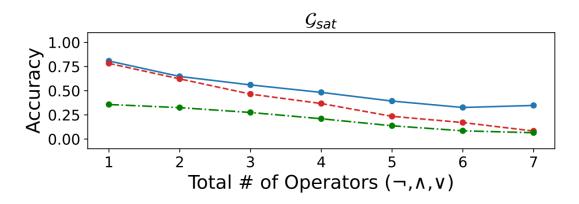


- Results with randomized versions of predicates
 - Eg: p1(o1) and p2(o1, o4)
- Performance of LLMs is about 50% for small formulae.

Results: English language-based predicates

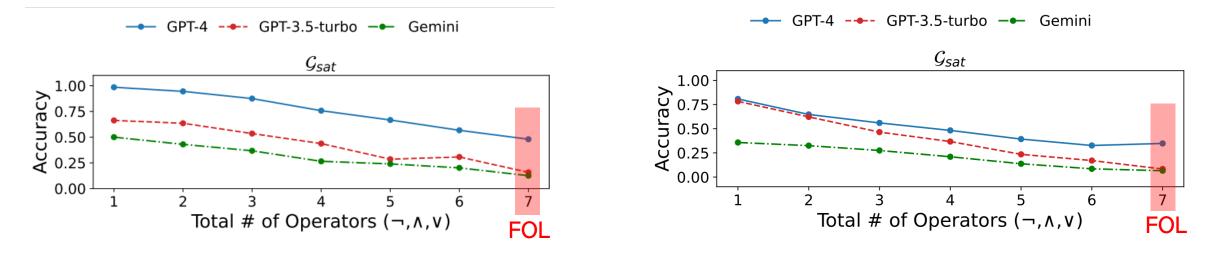
 $\begin{aligned} \mathcal{G}_{fol} &: f \to q, \dots s | s \\ q \to \forall \text{variable} | \exists \text{variable} \\ s \to \text{predicate} | \text{predicate}(t, \dots) | s \lor s | s \land s | \neg s \end{aligned}$ $\begin{aligned} \text{predicate} \to \text{Friends} | \text{Enemies} | \dots \\ t \to \text{constant} | \text{variable} \\ \text{constant} \to \text{John} | \text{William} | \dots \\ \text{variable} \to x_1 | x_2 | \dots \end{aligned}$

--- GPT-4 --- GPT-3.5-turbo --- Gemini

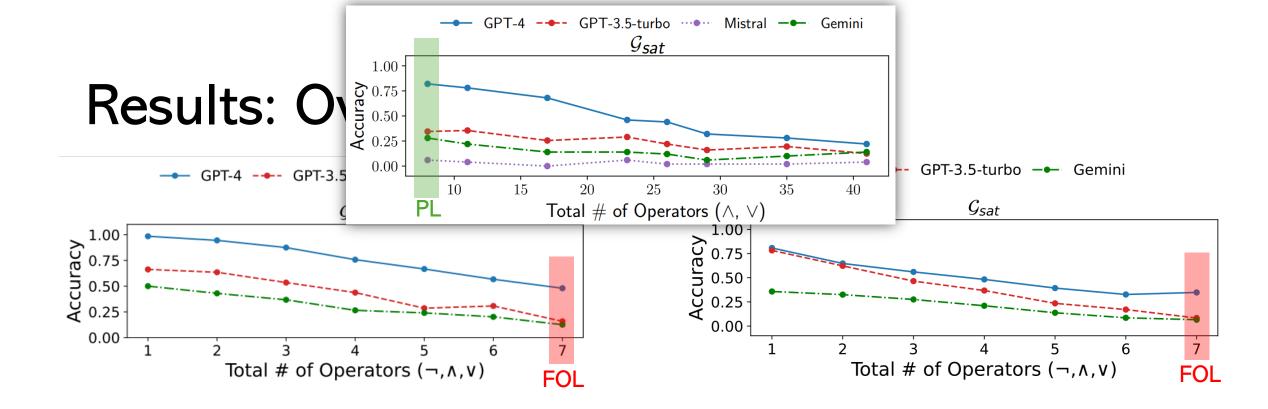


- Results with English language-based versions of predicates
 - Predicates were pulled from a vocabulary
- Slightly worse performance than randomized predicates

Results: Overall



- Our results show that LLMs cannot translate satisfactorily even for FOL
- Much worse than propositional logic (PL)
 - Results much worse, much earlier: at 7 #ops, accuracy=75% (50%) for PL (FOL)
 - In PL, we did not even count negations as operators!



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 - Results much worse, much earlier: at 7 #ops, accuracy=75% (50%) for PL (FOL)
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Conclusions

- We introduced an effective technique for assessing LLMs in the sphere of formal syntax
- Our approach is automatic and is developed on well-defined reasoning processes making it less susceptible to selfevaluation/critic based hallucinations

Future Work

• Expand coverage to different kinds of formal syntax: (e.g. PDDL)